

TMMF

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Parte 4 – Funzioni con MatLab

GRAPH OF $z=f(x,y)$

Consider a function of two real variables

$$f: A \subseteq \mathbb{R}^2 \rightarrow \mathbb{R}$$

We want to depict its **graph** (or **plot**)

To the scope there exist **two different ways** in MatLab:

1) PUNCTUAL DEFINITION

2) ANONYMOUS FUNCTION

1) Graph with punctual definition

The steps are the following

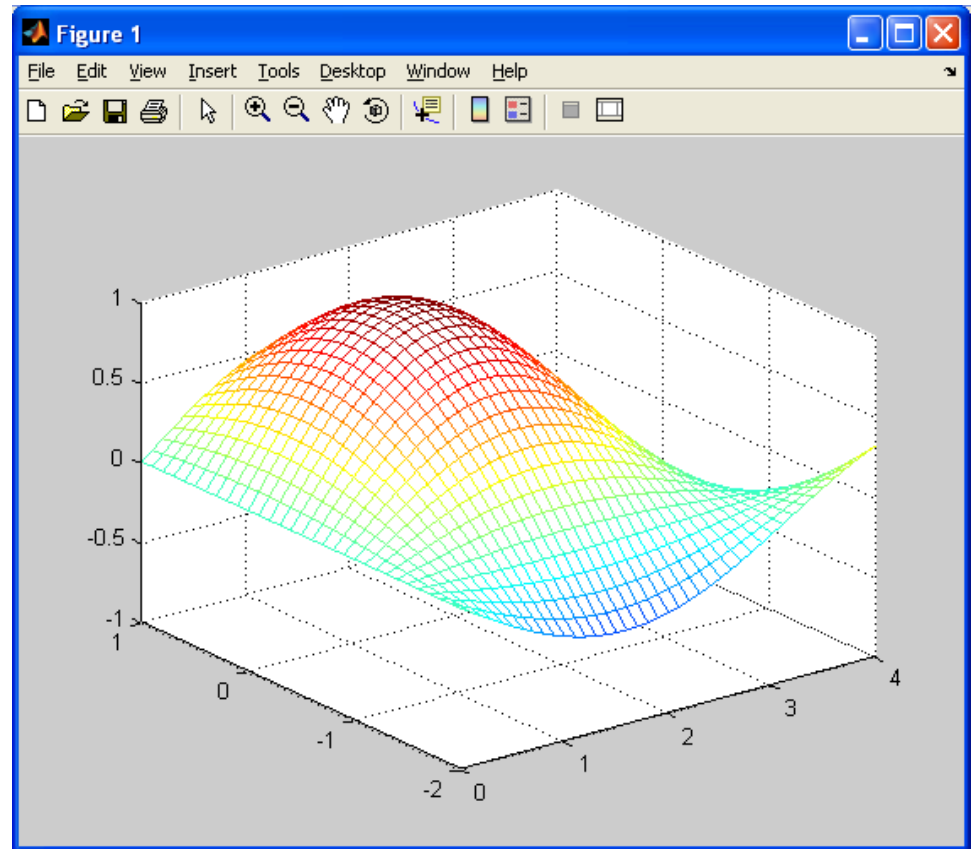
- a. **Define the interval of values that must be considered for the two independent variables.** The interval must be defined as row vectors, x and y , having an high number of equally spaced elements. Thus the operator `:` or `linspace` can be used.
- b. **Define a grid** on the plane (x,y) constituted by the set of couples having one element of the vector x and the second element taken from the vector y

the command `[X Y]=meshgrid(x,y)` creates matrices X and Y

- c. **Calculate the function $z=f(X,Y)$** by applying f to the matrices X and Y . The punctual operators and the syntax of elementary functions must be considered. In such a way the value associated to each couple (x,y) is computed
- d. **Depict the graph** of the function by using commands `surf(X,Y,z)` or `mesh(X,Y,z)` that plots the set of points (x,y,z) in \mathbb{R}^3

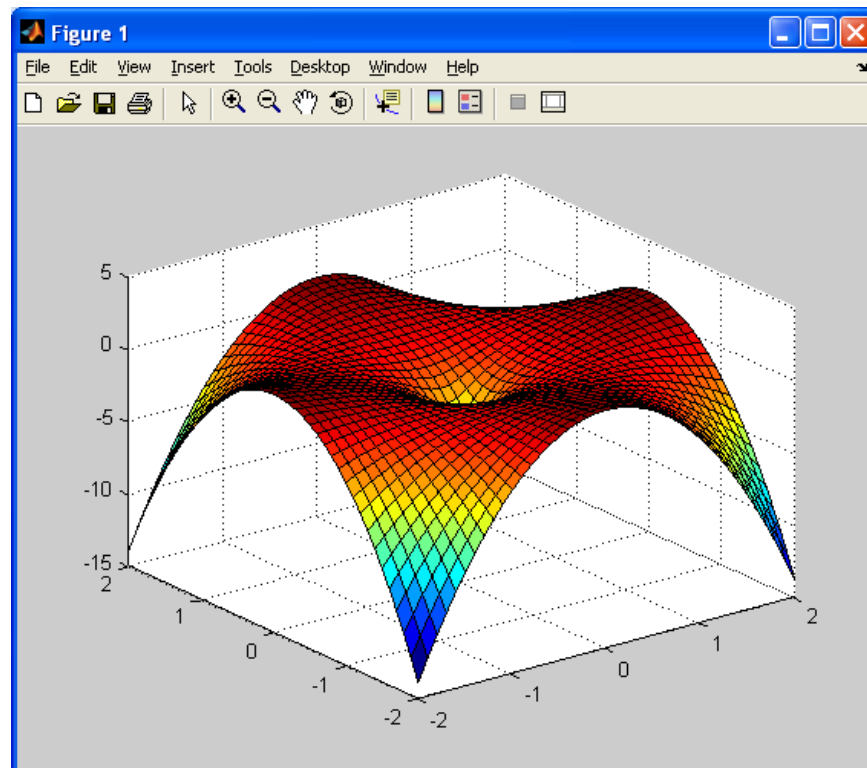
EX (1) $z = \sin(x) \cdot \cos(y)$

```
>> x=0:0.1:4;  
>> y=-2:0.1:1;  
>> [X Y]=meshgrid(x,y);  
>> z=sin(X).*cos(Y);  
>> mesh(X,Y,z)
```



EX (2) $z = \ln(x^2 + y^2) - x^2 y^2$

```
>> y=-2:0.1:2;  
>> x=-2:0.1:2;  
>> [X Y]=meshgrid(x,y);  
>> z=log(X.^2+Y.^2)-(X.^2).*(Y.^2);  
>> surf(X,Y,z)
```



EX 14

Plot the graphs of the following functions (punctual definition)

(1) $z = \ln(x) \cdot \ln(y)$

consider $x \in [1, 4]$ and $y \in [1, 4]$ and use mesh

(2) $z = x^2 + y^2 - \cos(x) - \cos(y)$

consider $x \in [-1, 1]$ and $y \in [-1, 1]$ and use surf

1) Graph with anonymous function

The steps are the following

- a. Define the anonymous function by using the following expression:

`z=@(x,y) law_of_xy`

thus $f(x,y)$ will be associated to z

Notice It is then possible to calculate the value of z at a given point (x_0,y_0) by using the command `z(x0,y0)`

- b. Depict the plot by using one of the following commands:

`ezsurf(z,[x_min x_max],[y_min y_max])` or

`ezmesh(z,[x_min x_max],[y_min y_max])`

and the graph will be represented for the independent variables belonging to the defined intervals

EX

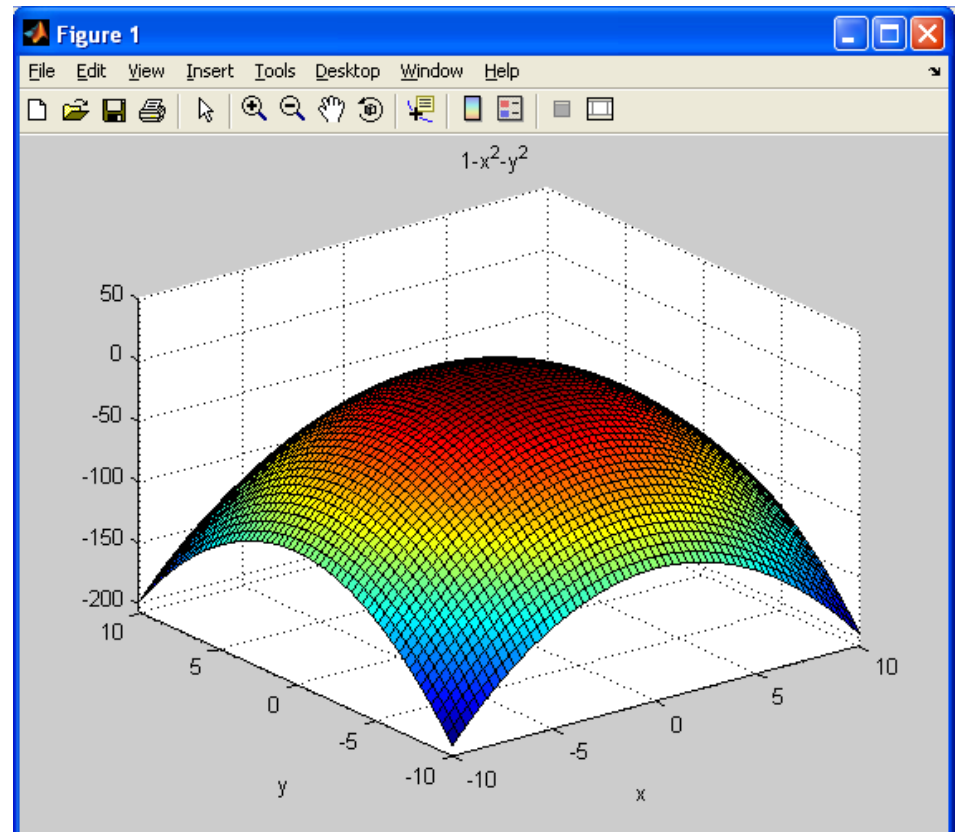
$$(1) \quad z = 1 - x^2 - y^2$$

```
>> z=@(x,y) 1-x.^2-y.^2;  
>> ezsurf(z,[-10 10],[-10 10]);
```

```
>> z(50,50)
```

```
ans =
```

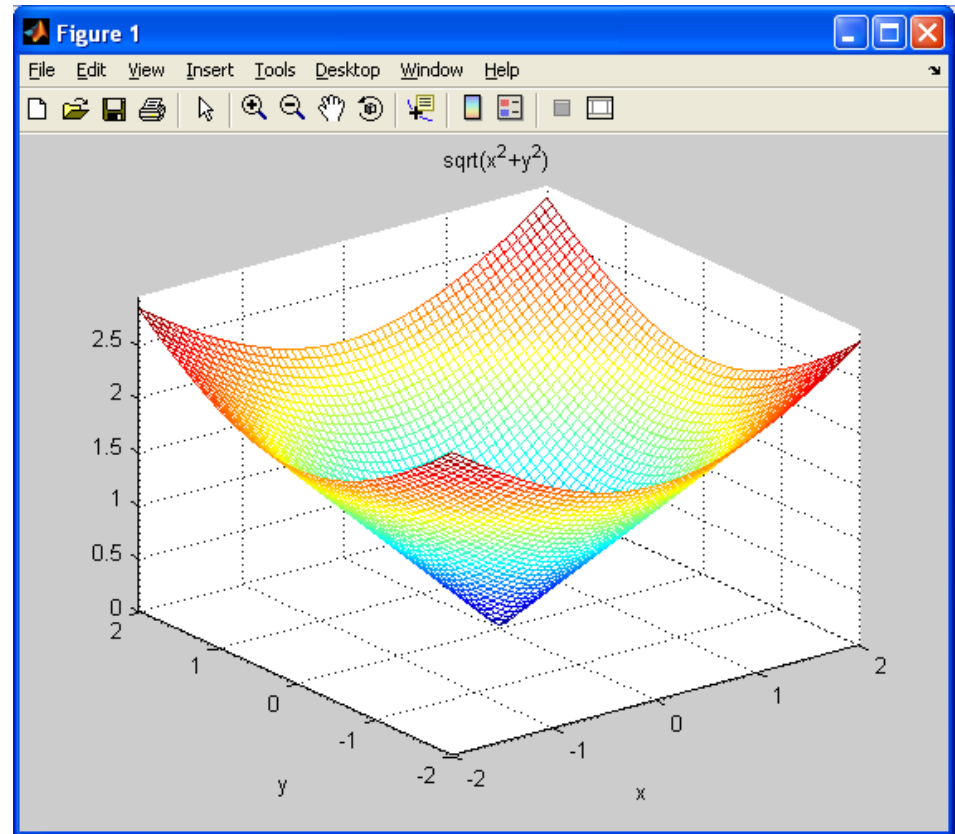
```
-4999
```



EX

$$(2) \quad z = \sqrt{x^2 + y^2}$$

```
>> z=@(x,y) sqrt(x.^2+y.^2);  
>> ezmesh(z,[-2 2],[-2 2]);
```



Visualisation options

Once the graph is obtained **the options related to the visualisation of the graph can be activated** and the tools of the graph-window can be used

- ❖ first **show plot tools** by activating View -> Palette, Browser, Editor
- ❖ click on the **surface** to modify its characteristic
- ❖ click on the **space** to modify the graph properties (such as title, labels, ticks and so on)

EX 15

Plot the graphs of the following functions (anonymous definition)

(1) $z = \sqrt{|x|} y^2 - |x|$ (use command ezsurf)

(2) $z = (xy)e^{x^2-y^2}$ (use command ezmesh)

Select a **suitable interval** for variables x and y

Adjust the obtained graphs by using the plot tools

LEVEL CURVES

The level curves of function $z=f(x,y)$ can be plotted with MatLab

1. Punctual definition

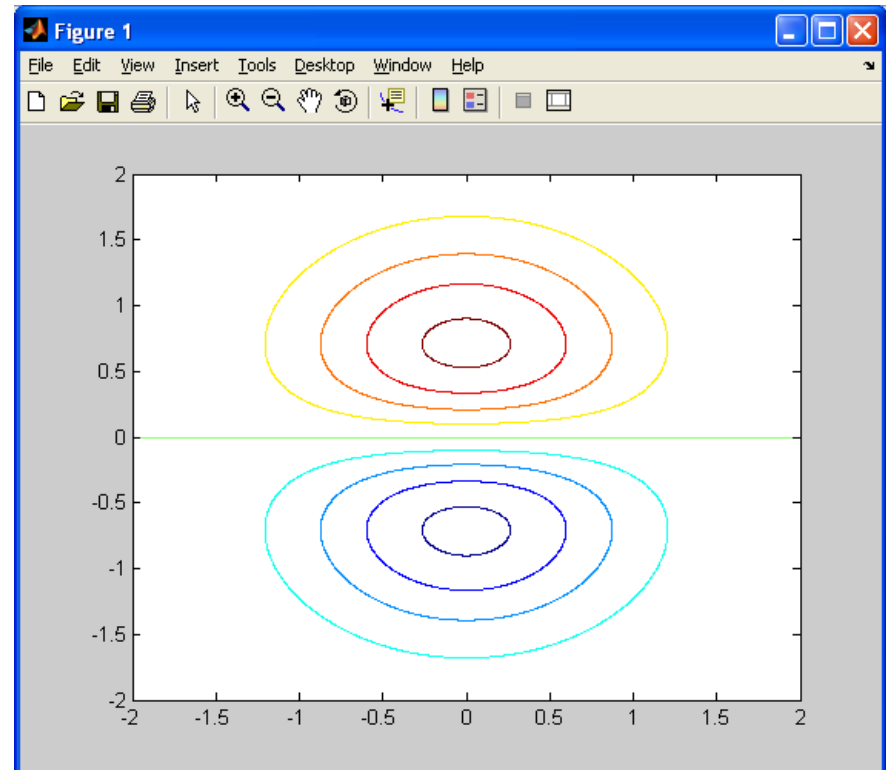
Define the function by discretization and then use the command

`contour(x,y,z)` (or `contourf(x,y,z)`) to obtain the level curves

EX

$$(1) \quad z = ye^{-x^2-y^2}$$

```
>> x=linspace(-2,2,1000);  
>> y=linspace(-2,2,1000);  
>> [X Y]=meshgrid(x,y);  
>> z=Y.*exp(-X.^2-Y.^2);  
>> contour(x,y,z);
```



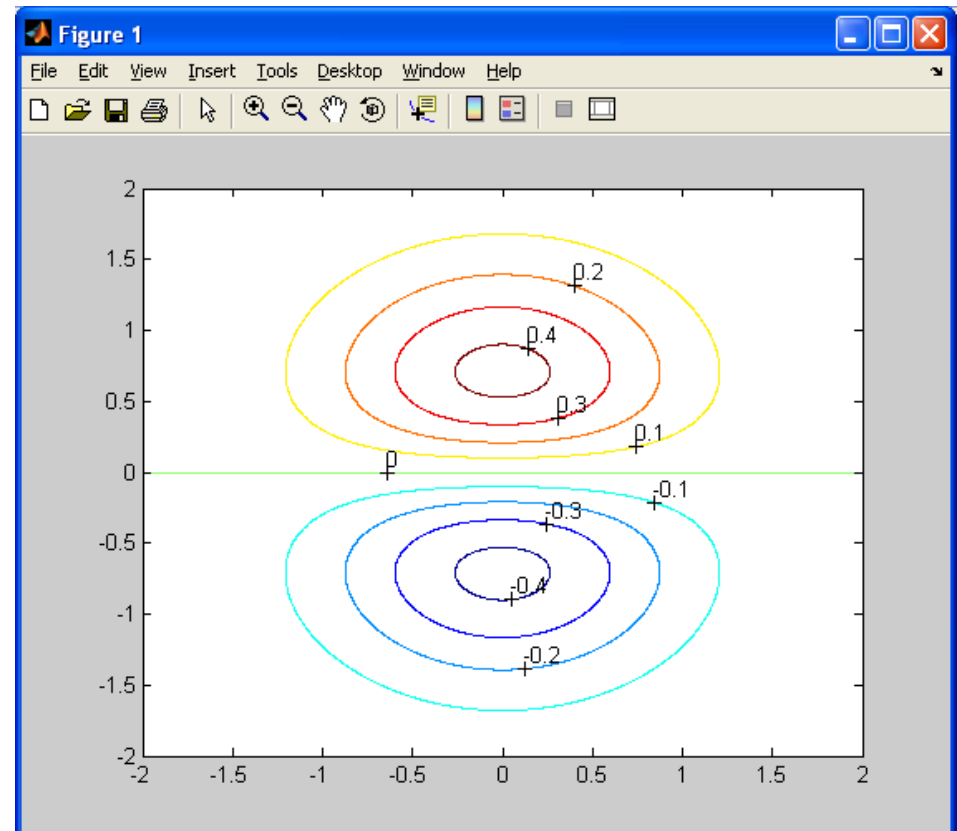
Notice: It is possible to add the z-value to each level curve

An output variable must be saved (for example c) while using the command contour:

`[c]=contour(x,y,z)`

With the instruction `clabel(c)` the z-value will be reported to each curve

```
>> [c]=contour(x,y,z);  
>> clabel(c);
```



EX 16

**Plot the level curves of the following functions (punctual definition);
choose opportune intervals**

(1) $z = \frac{1}{x^2 + y^2 + 1}$ (use command `contour`)

(2) $z = |\sin(x) + \cos(y)|$ (use command `contourf`)

LEVEL CURVES

2. Anonymous definition

Define the function as an anonymous function

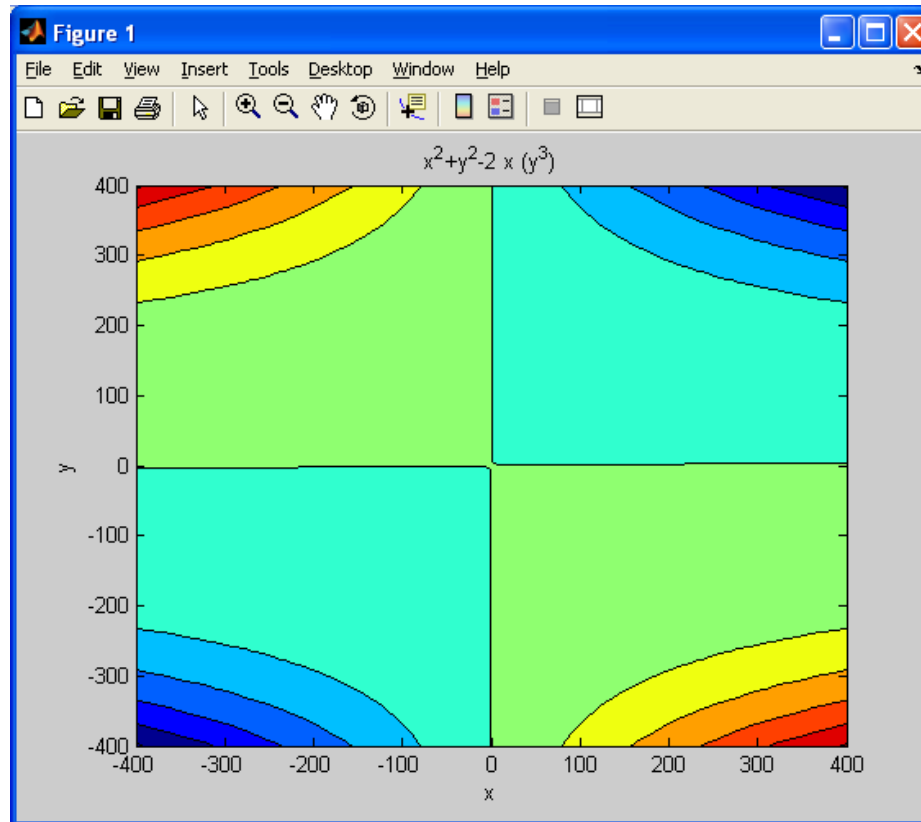
The command `ezcontour(z,[x_min x_max],[y_min y_max])`

(or `ezcontourf(z,[x_min x_max],[y_min y_max])`) must be used to plot the level curves

EX

$$(2) \quad z = x^2 + y^2 - 2xy^3$$

```
>> z=@(x,y) x.^2+y.^2-2*x.*(y.^3);  
>> ezcontourf(z,[-400 400],[-400 400]);
```



EX 17

Plot the level curves of the following functions by using the anonymous definition

$$(1) \quad z = \ln(|xy|) + \sqrt{x^2 + y^2}$$

$$(2) \quad z = x^2 + y^2 - 1$$

It is also possible to plot both the surface and the level curves in the 3D space

1. Punctual definition

Define the function and then use the commands `surf(x,y,z)` (or `meshc(x,y,z)`)

2. Anonymous definition

Define the function and then use the commands

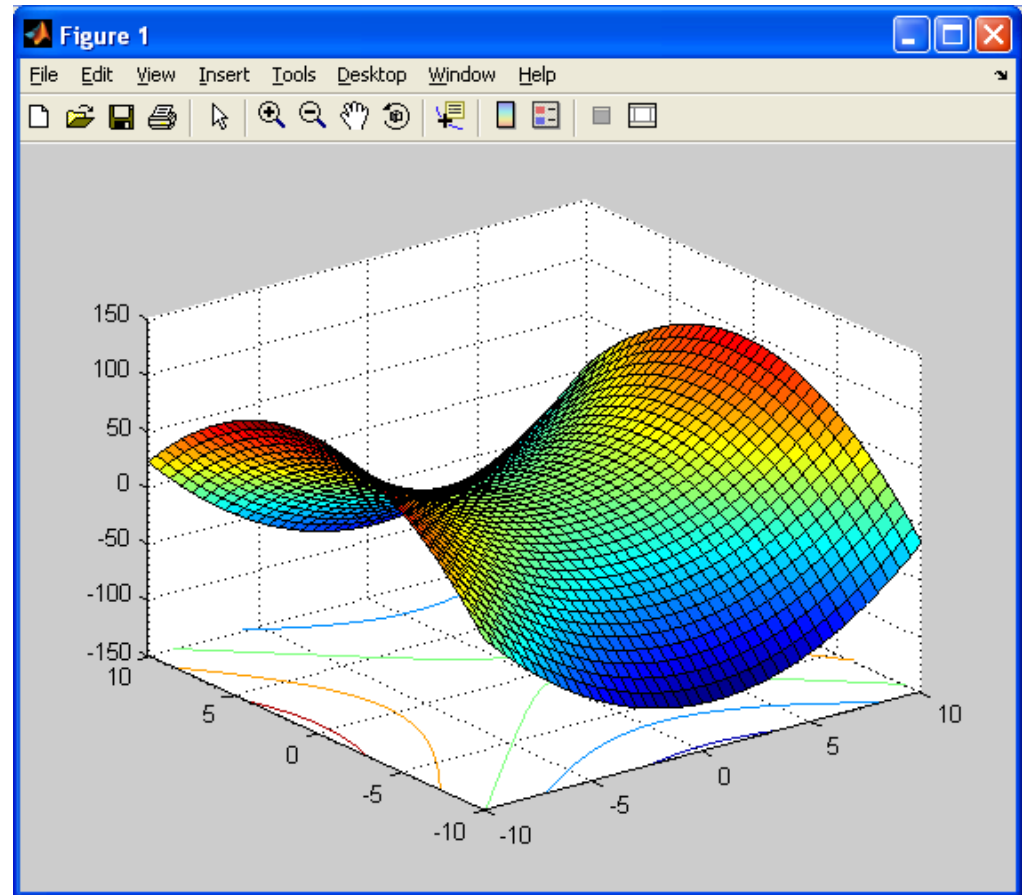
`ezsurf(z,[x_min x_max],[y_min y_max])`

(o `ezmeshc(z,[x_min x_max],[y_min y_max])`)

EX

$$(1) \quad z = x^2 - y^2 - x + 2 + y$$

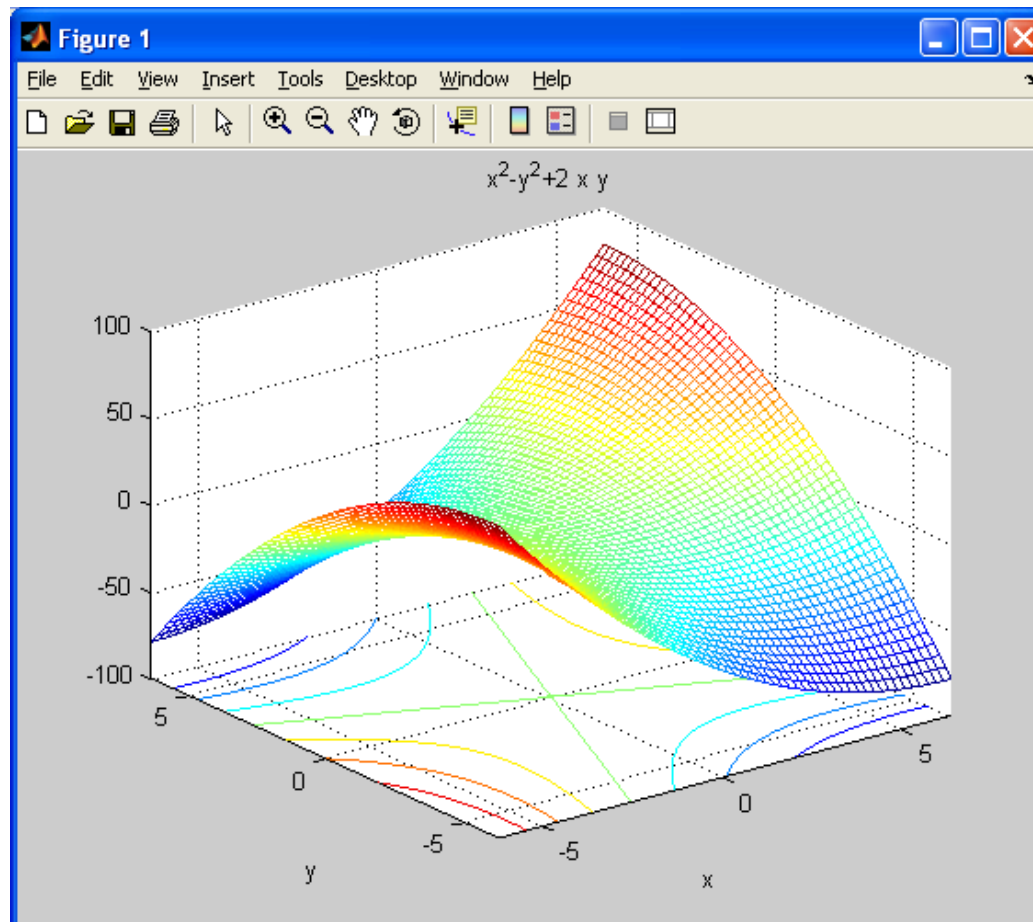
```
>> x=-10:0.5:10;  
>> y=-10:0.5:10;  
>> [X Y]=meshgrid(x,y);  
>> z=X.^2-Y.^2-X+2+Y;  
>> surfc(x,y,z);
```



EX

$$(2) \quad z = x^2 - y^2 + 2xy$$

```
>> z=@(x,y) x.^2-y.^2+2*x.*y;  
>> ezmeshc(z);
```



PLACE GRAPHS SIDE BY SIDE

It is also possible to plot two graphs side by side

Once a graph is obtained, by using the tool of the figure-window, it is possible to select the **new subplots** options



Then one of the plots can be selected: all the commands given in the command window will be applied to the selected plot. Change selection to apply command to a different plot

Notice: the command **axis square** can be used to obtain a square plot area

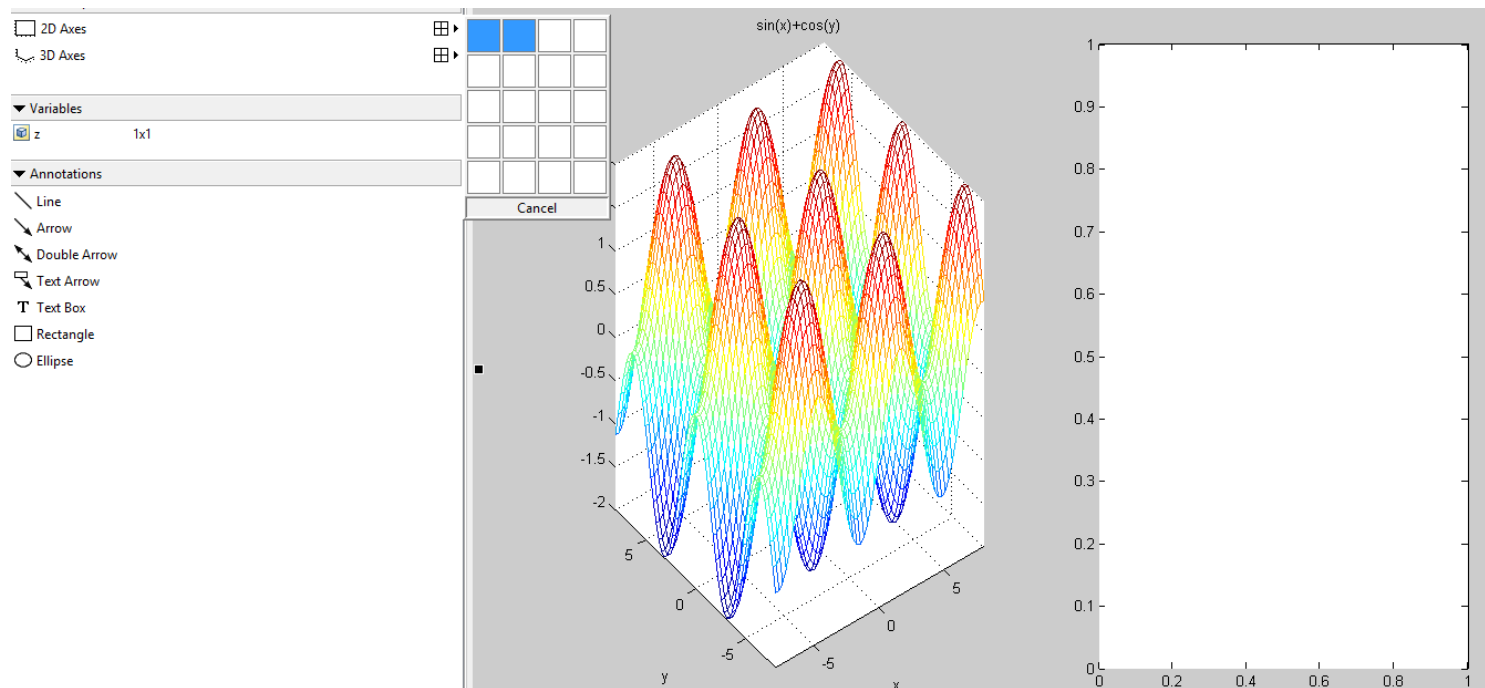
EX

Plot the graph of the following function and put the level curves on the right hand side

$$z = \sin x + \cos y$$

1) Fristly **plot the graph** and then select a second subplot

```
>> z=@(x,y) sin(x)+cos(y);  
>> ezmesh(z,[-8 8],[-8 8])
```



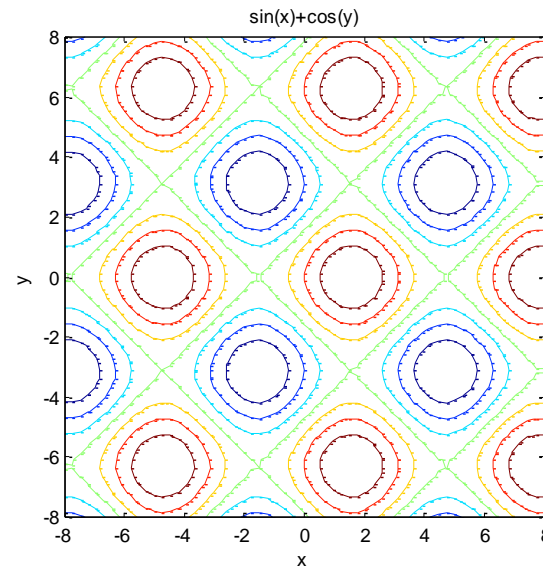
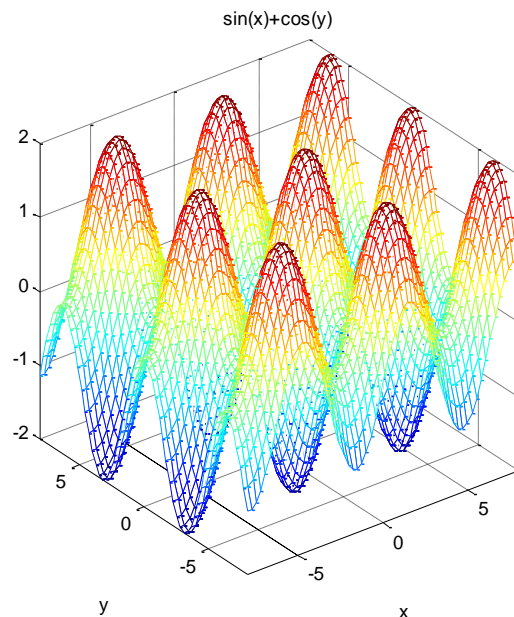
2) Select the second subplot and give instruction on the command window

```
>> ezcontour(z,[-8 8],[-8 8])
```

Once obtained the second plot, select the first one and give command

```
>>axis square
```

And do the same with the second graph!



Notice: the figure can be saved in several formats, for instance jpg

EX 17

Plot the graphs and the level curves (side by side) of the following functions

(1) $z = \sqrt{|x^2 - y^2|} + ye^{x^2+y^2}$ (use the anonymous definition)

(2) $z = x^2 + y^2 - xy$ (use the puntual definition)

Homeworks

1.9

Consider the following two functions

$$(1) \quad z = x^2 - y^2 - 5xy$$

$$(2) \quad z = \sqrt{x^2 + y^2 - 3}$$

- Calculate the value of z for $x=12$ and $y=-2$ for both functions
- Plot the graph of function (1) together with its level curves and then put on the right hand side the graph of function (2)
- Adjust the graph by using the plot tools and save the final figure in jpg format

Notice that: it is necessary to use the anonymous definition!

Homeworks

1.10 Consider the following function

$$z = \log |x^2 y|$$

- Plot the graph and then put the level curves on the right hand side by specifying the z values

Notice that: it is necessary to use the punctual definition!

Homeworks

1.11 Consider the following linear utility function

$$y = 0.5x_1 + 0.2x_2$$

- Plot the graph and then put the indifference curves on the right hand side

Notice that: (1) the indifference curves are the level curves; (2) being an economic function only not-negative values of x and y must be considered!

Homeworks

1.12

Consider the following CES production function

$$z = 2(3x^{-0.5} + 0.5y^{-0.5})^{-0.2}$$

- Plot the graph and then put the isoquants on the right hand side

Notice that: being an economic function only not-negative values of x and y must be considered!