

University of Macerata  
Mathematical Methods for Economics and Finance

Exam Simulation

May 08, 2024

1. Financial mathematics:

- We have 500 euro today and we want to invest this amount for 6 years with simple interest rule. For the first 3 years it is applied the interest rate of 8% while for the last 3 years it is used  $i_4 = 0.01$ . Determine the final value of the investment.
- Consider 1000 euro disposable at time  $t = 2$  and a monthly interest rate of 0.5% with the exponential interest rule. Determine the equivalent amount of money at times  $t = 1.5$  and  $t = 6$ .

2. In Matlab:

- Define the vector  $\mathbf{v}$  as the vector whose elements are the integer numbers from 1 to 20.
- Set the elements in odd position equal to -1 and store the result again in the vector  $\mathbf{v}$ .
- Set the elements in even position equal to the respective elements of the array of integers ranging from 10 to 1 and store the result again in the vector  $\mathbf{v}$ .
- Starting from the vector  $\mathbf{v}$ , form four vectors  $\mathbf{v}_1$ ,  $\mathbf{v}_2$ ,  $\mathbf{v}_3$ , and  $\mathbf{v}_4$ , where  $\mathbf{v}_i$  (with  $i \in \{1, 2, 3, 4\}$ ) is the  $i$ -th quarth of the vector  $\mathbf{v}$ .
- Create the matrix  $\mathbf{A}$  whose rows are the vectors  $\mathbf{v}_1$ ,  $\mathbf{v}_2$ ,  $\mathbf{v}_3$ , and  $\mathbf{v}_4$ .
- Create the matrix  $\mathbf{B}$  whose columns are the vectors  $\mathbf{v}_1$ ,  $\mathbf{v}_2$ ,  $\mathbf{v}_3$ , and  $\mathbf{v}_4$ .
- Let  $\mathbf{C}$  be the matrix  $\mathbf{A}$  without the first row and the first column.
- Let  $\mathbf{D}$  be the matrix  $\mathbf{B}$  without the last row and the last column.
- Compute  $\mathbf{E} = \mathbf{C} + \mathbf{D}^T$ .
- Let  $f(x) = \sqrt{|x|} \cos x$  and  $g(x) = \frac{x^2}{e^x}$ . Create a subplot with the graph of  $f$  in the first subplot and the graph of  $g$  in the second subplot. The two graphs should be in the interval  $[-6, 6]$ .

- Is it possible to compute  $f(\mathbf{D}) + g(\mathbf{E})^T$ ? If so, store the result in a new matrix  $\mathbf{F}$ .
3. Graphically sketch the domain of the function

$$f(x, y) = \frac{\sqrt{2-x-y}}{y-x} + \ln [4 - (x-2)^2 - (y-2)^2] .$$

4. Consider the function

$$f(x, y) = e^{2x-3y}.$$

After graphing the function, find the second-order Taylor polynomial of  $f$  centered at  $\mathbf{x}_0 = (1, 0)$ .

5. Manually find the eigenvalues of the following matrix:

$$\mathbf{C} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -2 & 1 \\ 1 & 2 & 1 \end{bmatrix} .$$

Moreover, find an eigenvector associated to each eigenvalue. Finally, check your results in Matlab.